

# *Determination of Mean Free Path of Quantum/Waves and Total Emissivity of the Carbon Dioxide Considering the Molecular Cross Section.*

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## *Abstract:*

Through the application of astrophysical formulas, the mean free path length of a Quantum/wave stream leaving the surface of the Earth to the outer space before it has collided with a molecule of carbon dioxide and its total emissivity are calculated. The output of this algorithm indicates a value of about 33 meters. Also calculated is the time taken by a Quantum/wave to exit the atmosphere after it has collided with a molecule of carbon dioxide — which is 5 milliseconds (ms).

## *Introduction:*

Carbon dioxide (CO<sub>2</sub>) is vitally important molecule for life on Earth. Carbon dioxide molecules are taken in from the atmosphere by photosynthetic organisms which employ them to build more complex substances that are used for storing the energy transferred from the quantum/waves to the molecules of chlorophyll.

The current assessment demonstrates that CO<sub>2</sub> is so well dispersed throughout the bulk volume of the atmosphere that its efficiency for capturing quantum/waves emitted from the surface is extremely low.

The objectives of this didactic article are to demonstrate that the mean free path length of the Quantum/wave stream does not significantly change the total emissivity of the CO<sub>2</sub> and that the time taken by a Quantum/wave to exit the atmosphere to space, without colliding with a molecule of CO<sub>2</sub>, is extremely low.

## *Methodology*

I have introduced the molecular cross section of the carbon dioxide  $\sigma_{CO_2mol}$ , in which case a value for  $n$ , calculated from the molar density of the carbon dioxide and the number of molecules per mol of the substance was demanded to make the most accurate solution.

$$\alpha = (\varepsilon/\varepsilon b) = \varepsilon$$

## *Analysis*

Preliminary Data:

The density of the gas carbon dioxide in the atmosphere is obtained by the following formula:

$$\rho_{CO_2} = (12.187 * \text{Molar mass of } CO_2 * \text{volumetric fraction of } CO_2) \div (276.69 K) = 756 \text{ mg/m}^3. ^7$$

Where 12.187 is the molar mass of elemental carbon, molar mass of carbon dioxide is 44.01, and the volumetric fraction of CO<sub>2</sub> is 390 ppmV and 276.69 K is for temperature.

To introduce this value into the formula that I will describe below, I made use of the following important magnitudes:

$$\rho_{CO_2} = 756 \text{ mg/m}^3 = 0.756 \text{ g/m}^3 = 7.56 \times 10^{-7} \text{ g/cm}^3$$

$7.56 \times 10^{-7} \text{ g/cm}^3$  is the density of the atmospheric carbon dioxide in the atmosphere obtained from the following calculation:

$$\rho_{CO_2} = (12.187 \text{ of } ^{12}\text{C} * MM_{CO_2} * MF_{CO_2}) \div T_{abs}$$

Where 385 ppmV is  $MF_{CO_2}$ , 44.01 are for  $MM_{CO_2}$  and 276.69 K is  $T_{abs}$ . You can make your own calculations at LENNTECH<sup>(7)</sup>, calculator online.

$$\text{Mass of } CO_2 \text{ per cm}^3 \text{ of air} = 7.56 \times 10^{-7} \text{ g/cm}^3 * 1 \text{ cm}^3 = 7.56 \times 10^{-7} \text{ g.}$$

Avogadro's number =  $6.02 \times 10^{23} \text{ molecules/mol}$  (Avogadro's number has not units, however, when it is introduced like a constant it is expressed as  $6.02 \times 10^{23} / \text{mol}$ ).<sup>13</sup>

$$CO_2 \text{ Molar Density} = 44.01 \text{ g} / 22261 \text{ cm}^3 = 0.001977 \text{ g/cm}^3.$$

$$\text{Molar mass of } CO_2 = 44.01 \text{ g}$$

$$\text{Number of moles of } CO_2 = (\text{mass in } 1 \text{ cm}^3 \text{ of air}) / (\text{molar mass}) = 7.56 \times 10^{-7} \text{ (g)} / 44.01 \text{ (g/mol)} = 1.7178 \times 10^{-8} \text{ moles}$$

$$\text{Number of molecules of carbon dioxide per gram} = \text{moles} * \text{Avogadro's number} / \text{molar mass} = (1.7178 \times 10^{-8} \text{ moles}) * (6.02 \times 10^{23} \text{ molecules/mol}) / 44.01 \text{ g} = 2.35 \times 10^{14} \text{ molecules/mol.}$$

Considering the density of  $CO_2$  in the atmosphere, the number of moles of carbon dioxide measured in one cubic centimeter in the atmosphere mass,  $1.7178 \times 10^{-8} \text{ moles}$  are contained in  $7.56 \times 10^{-7} \text{ g}$  of carbon dioxide per each cubic centimeter of the current atmosphere.

$$CO_2 \text{ molecule's cross section } (\sigma) = 5 \times 10^{-22} \text{ cm}^2$$

*Determination of the Mean Free Path Length of quantum/waves in the atmosphere before colliding with a molecule of carbon dioxide.*

Formula to calculate the mean free path length of quantum/waves before colliding with molecules of  $CO_2$ :

$$l = m / (n \sigma) \text{ (References 1 and 2).}$$

Where  $l$  is for the mean free path length,  $m$  is for the mass of the gas measured in one cubic centimeter of air,  $n$  is the effective quantum density, and  $\sigma$  is the cross section of a molecule of  $CO_2$  before vibrational dephasing ( $\sigma = 5.0 \times 10^{-22} \text{ cm}^2$ ).

[Notice that  $n$  is the total number of states per volume unit, cubic centimeters in this case: according to quantum mechanics, to obtain the effective density we must to multiply the number of molecules per mol by the molar gas density of the carbon dioxide and consider other parameters,  $n = N_C * (e^{-((E_C - E_F)/kT)})$ . If we introduce an incorrect effective density, the results will be infinite numbers that have nothing to do with reality. In this instance, I have applied the short procedure for simplification and more clarity of the text].

*Known data:*

$CO_2$  molecule's cross section =  $5 \times 10^{-22} \text{ cm}^2$

Mass of  $CO_2$  (m) corresponding to a mass fraction of 390 ppmV =  $7.56 \times 10^{-7} \text{ g}$

*Effective molar density of carbon dioxide:*

$n/\text{mol}$  = molar gas density of carbon dioxide x Number of molecules per mole

The molar gas density of molecular carbon dioxide is obtained by the following formula:

$$\text{Molar gas } \rho_{CO_2} = MM_{CO_2} / MV_{STP}$$

Where  $MM_{CO_2}$  is molar mass of the carbon dioxide and  $MV_{STP}$  is the molar volume of any gas at STP (22.4 L).

Introducing magnitudes:

$$\text{Molar gas } \rho_{CO_2} = 44.01 \text{ g} / 22.4 \text{ L} = 1.9647 \text{ g/L} = 0.0019647 \text{ g/cm}^3$$

And the effective molar density ( $n/\text{mol}$ ) of carbon dioxide in one cubic centimeter is:

$$n/\text{mol} = (2.35 \times 10^{14} / \text{mol}) (0.0019647 \text{ g/cm}^3) = 4.617045 \times 10^{11} \text{ g / mol cm}^3$$

Solving for n, we obtain:

$$n = (2.35 \times 10^{14} / \text{mol}) (0.0019647 \text{ g/cm}^3)(\text{mol}) = 4.617045 \times 10^{11} \text{ g / cm}^3$$

Therefore,  $4.617045 \times 10^{11} \text{ g / cm}^3$  is the effective molar density that must be considered to calculating the mean free path length of a quantum/wave crossing the troposphere between collisions with molecules of carbon dioxide.

Determination of the Mean Free Path Length of Quantum/Waves through the Earth's troposphere.

*Introducing magnitudes:*

$$l = (7.56 \times 10^{-7} \text{ g}) / (4.617045 \times 10^{11} \text{ g / cm}^3 * 5 \times 10^{-22} \text{ cm}^2) = 3275 \text{ cm}$$

$$l = 32.75 \text{ m}$$

Therefore, the mean free path of the surface quantum/waves stream (l) is 3275 cm, which is the trajectory of a quantum/wave passing through the atmosphere before it collides with a molecule of carbon dioxide.

This means that a quantum/wave shifts about 33 meters to hit onto a molecule of carbon dioxide in the atmosphere.

This enormous distance is well understood if we take into account that as the temperature of the lower troposphere increases during daylight by a highly energized surface quantum/wave stream, the thermal diffusivity of carbon dioxide increases, to be precise, as the temperature increases, the molecules diffuse more quickly into a thermally expanded volume of air.

In consequence, the distance between one molecule of carbon dioxide and another molecule of carbon dioxide is lengthened as the temperature increases. For example, the thermal diffusivity of the carbon dioxide at 255 K (-18 °C or -0.40 F) is  $7.83 \times 10^{-6} \text{ (m}^2/\text{s)}$ , while at 308 K (35 °C, or 95 F) is  $1.171 \times 10^{-5} \text{ (m}^2/\text{s)}$ .<sup>14</sup>

*Determination of the time a quantum/wave takes to leave the atmosphere of the Earth towards space after colliding with molecules of CO<sub>2</sub>:*

Formula for obtaining the time taken by a Quantum/wave to leave the Earth's atmosphere after colliding with molecules of CO<sub>2</sub>:

$$t = r^2 / (l * c) \text{ (References 1 and 2)}$$

Known Data:

$$r \text{ trop.} = 700000 \text{ cm}$$

$$l = 3275 \text{ cm}$$

$$c = 2.99909301 \times 10^{10} \text{ (cm/s)}$$

Introducing Magnitudes:

$$t = r^2 / (l * c) = 4.9 \times 10^{11} \text{ cm}^2 / [3275 \text{ cm} * 2.99909301 \times 10^{10} \text{ (cm/s)}] = 0.004989 \text{ s}$$

$$t = 0.004989 \text{ s}$$

The result indicates that it takes quantum/waves approximately 5 ms (*milliseconds*) to cross the troposphere from the surface of the Earth after colliding with or being scattered by molecules of CO<sub>2</sub>.

In contrast, molecules of Water Vapor (H<sub>2</sub>O) and solid particles which are also present in the atmosphere, intercept and absorb the quantum/waves emitted from the surface of the Earth long before they could collide with any molecules of carbon dioxide and before the molecules of carbon dioxide interact with other molecules (due to the very low CO<sub>2</sub> cross section):

*Determining the Total Emissivity of the Atmospheric Carbon Dioxide as from the Crossing Time Lapse that a Quantum/Wave takes to leave the Troposphere*

The formula to calculate the total emissivity of a gas or plasma is as follows:

$$\varepsilon = (1 - e^{(t * (-1/s))}) / \sqrt{\pi}$$

Where  $\varepsilon$  is the total emissivity and  $t$  is the crossing time lapse of a quantum/wave.

Known values:

$$t = 0.004989 \text{ s}$$

Introducing magnitudes:

$$\varepsilon = (1 - e^{(0.004989 \text{ s} * (-1/s))}) / (\sqrt{3.1415...}) = 0.0028077$$

This result is in accord with the result obtained by considering the partial pressure of the carbon dioxide and its instantaneous temperature in the atmosphere; additionally, it coincides with the total emissivity of **almost zero** obtained from the experiments conducted by H. C. Hottel<sup>8</sup>, B. Leckner<sup>9</sup>, M. Lapp<sup>10</sup>, C. B. Ludwig<sup>11</sup>, A. F. Sarofim<sup>12</sup> and their collaborators<sup>11, 12</sup>

#### CONCLUSIONS:

The results obtained by experimentation coincide with the results obtained by applying astrophysics formulas. Therefore, both methodologies are reliable to calculate the total emissivity/absorptivity of any gas of any planetary atmosphere.

At an average density, the atmospheric water vapor allows quantum/waves to cross the troposphere to the tropopause in 0.004989 s, i.e.  $\sim 5$  milliseconds. Through comparing the ability of water vapor to avoid the quantum/waves to escape towards the outer space with that of CO<sub>2</sub> (0.004989 s), we can affirm that the role of CO<sub>2</sub> on warming the atmosphere or the surface is impossible according to Physics Laws.

If we consider also that the carbon dioxide has by far a lower total absorptivity and total emissivity than water vapor, we fairly conclude that carbon dioxide is not a driver of climate changes or global warming on the planet Earth.

The low thermal diffusivity of carbon dioxide makes of it to be an inefficient substance to adjust its temperature to that of its surroundings. Consequently, the carbon dioxide can never reach the thermal equilibrium with respect to the remainder molecules of the air. In consequence, **carbon dioxide is not a greenhouse gas.**

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